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Report Number:
96-069

Arnaud, Denis and Szpankowski, Wojciech, "Pattern Matching Image Compression with Predication Loop: Preliminary Experimental Results" (1996). *Department of Computer Science Technical Reports*. Paper 1323.
<https://docs.lib.purdue.edu/cstech/1323>

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**PATTERN MATCHING IMAGE COMPRESSION
WITH PREDICATION LOOP:
PRELIMINARY EXPERIMENTAL RESULTS**

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**CSD-TR 96-069
November 1996**

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Preliminary Experimental Results

November 11, 1996

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Abstract

Recently, a novel image compression technique based on pattern matching was proposed, namely *Pattern Matching Image Compression* (PMIC). Basically, it is a lossy extension of the well known Lempel-Ziv scheme. It was proved that such an extension leads to a suboptimal compression, and that the compression ratio can be as low as the so called Rényi entropy. Success of PMIC crucially depends on several enhancements such as searching for reverse approximate matching, recognizing substrings in images that are additively shifted versions of each other, introducing a variable and adaptive maximum distortion level, and so forth. In this paper, we introduce another enhancement, namely, predictive coding. More importantly, we implement *Differential Predictive Code Modulation* (DPCM) within PMIC scheme. We report here some preliminary experimental results which show that PMIC enhanced by prediction can improve compression ratio for good quality images as well as speed of compression for PMIC.

*This work was supported by NSF Grants NCR-9415491 and CCR-9201078.

1 Introduction

These days most media are represented in a digital form, hence for data compression it is natural to apply a technique that was proved successful for inherently digital media such as text, namely Lempel-Ziv type schemes (cf. [17, 18]). In [8, 9] we propose to extend Lempel-Ziv approach to lossy (approximate) compression. While it is known that lossless Lempel-Ziv is asymptotically optimal (i.e., its compression ratio is asymptotically equal to the source entropy), in [9] Łuczak and Szpankowski (cf. also [16]) proved recently that a lossy extension of Lempel-Ziv scheme (of low complexity) is suboptimal, that is, it attains the compression ratio equal to the so called generalized Rényi entropy (instead of the optimal rate-distortion).

Using this theoretical underpinning, Atallah, Genin and Szpankowski [2] have recently implemented for image compression the above idea enhanced by some salient features discussed below. This novel scheme is called *Pattern Matching Image Compression* (PMIC), and it is briefly review in the next section (see also [4] for another implementation of a lossy Lempel-Ziv'78 scheme, however, in [4] there is no theoretical justifications for the reported results). In [2] it was concluded that for images of good quality PMIC scheme is competitive to JPEG and wavelet image compression. Superiority of PMIC at decompression (which does not require any computations since it basically only reads data) may turn out to be a crucial advantage in practice where asymmetric compression/decompression is a desirable feature (e.g., off-line video).

The central theme of the above approach is the notion of approximate repetitiveness. That is, if a portion of data almost-occurs five times, perhaps in close proximity but not necessarily contiguously, then we need only store the first such occurrence: The other four can be stored as (direct or indirect) references to the first occurrence. Somewhat surprisingly, this theme of exploiting approximate repetitiveness is uniformly useful to multimedia data, hence applies to text as well as to image, video, and audio data. However, the approximate repetitiveness can be hidden in various forms for different types of media (so one must consider different distortion measures). This is in contrast with current technology, where a different approach is used for each of these types of data (e.g., text and images). We plan to explore it in our future research.

In [2] several *enhancements* were introduced to the basic idea of PMIC that were instrumental for achieving good results. For example: searching for reverse approximate matching, recognizing substrings in images that are additively shifted versions of each other, introducing a variable and adaptive maximum distortion level, and so forth. These enhancements

are crucial to the overall quality of our scheme, and their efficient implementation leads to algorithmic results of interest in their own right. In this paper, we introduce one more enhancement, namely prediction that – as we shall see – will lead to shorter compression time and better compression ratio without significantly deterioration of image quality. Actually, we propose a more ambitious plan, namely implementing DPCM (i.e., Differential Predictive Code Modulation) within PMIC.

To see possible advantage of this new enhancement, we should observe that differential image (composed of the difference between the original image and its prediction) is much less correlated than the original one. Thus, any compression algorithm should gain in performance when applied on the differential image, instead of on the original one. However, for lossy compression there is a need to perform a *prediction loop* as explained in details in Section 3. In DPCM, this prediction loop is performed on each pixel, one by one. Thus, the implementation of a predictive feature for such a scheme as PMIC needs a few adaptations, because PMIC treats several pixels at a time, and does not work on a pixel-by-pixel basis.

The main idea to use a predictive loop in PMIC is that what is the basic cell for DPCM, namely one pixel, becomes the longest prefix found in the database for PMIC. As in DPCM, the differential image is quantized, thus allowing a slight increase in the compression ratio. Besides, although a differential image is significantly less correlated than the original image, it is still slightly correlated. This is because the low-order, linear predictor typically used here or in DPCM is suboptimal. But, while a Huffman coding scheme would not take advantage of this remaining correlation, since it encodes each differential value independently of its neighboring values, the PMIC scheme does, because it is a context based scheme. Thus, PMIC can achieve a bit rate potentially smaller than the zeroth-order entropy of the differential image. We report in this paper our implementation and preliminary experimental results.

2 Review of PMIC

This section is based on Atallah *et al.* [2]. The reader might also want to consult [8, 9, 13, 16] for theoretical background.

The detection of the above-mentioned approximate repetitiveness is done by approximate pattern matching, whence the name *Pattern Matching Image Compression* (PMIC). The main idea behind it is a lossy extension of the Lempel-Ziv data compression scheme in which one searches for the longest prefix of an uncompressed file that *approximately* occurs in the already processed file. The distance measure subtending the notion of approximate

occurrence can be the *Hamming distance*, or of the *square error distortion*, or the *string edit distance*, or any of the other distances considered in the distortion theory (cf. [3]).

In short, let us consider a stationary and ergodic sequence $\{X_k\}_{k=1}^{\infty}$ taking values in a finite alphabet \mathcal{A} (think of $\{X_k\}$ as an image scanned row by row). For image compression the alphabet \mathcal{A} has size $|\mathcal{A}| = 256$. We write X_m^n to denote $X_m X_{m+1} \dots X_n$, and for simplicity $X^n = X_1 \dots X_n$. The substring X_1^n is called *database sequence* or *training sequence* (and it represents already compressed image to which we make references while compression the remaining part of the image). We encode X_1^n into a compression code C_n , and the decoder produces an estimate \hat{X}_1^n of X_1^n . As a fidelity measure, we consider any distortion function $d(\cdot, \cdot)$ that is subadditive, and that is a *single-letter fidelity measures*, that is, such that $d(x^n, \hat{x}^n) = \frac{1}{n} \sum_{i=1}^n d(x_i, \hat{x}_i)$. Examples of fidelity measures satisfying the above conditions are: *Hamming distance*, and the *square error distortion* where $d(x_i, \hat{x}_i) = (x_i - \hat{x}_i)^2$. As in Luczak and Szpankowski [8, 9] we define the depth L_n as the length of the longest prefix of X_{n+1}^{∞} (i.e., uncompressed image) that approximately occurs in the database (i.e., already compressed image). More precisely, for a given $0 \leq D \leq 1$ we define: *Let L_n be the length k of the longest prefix of X_{n+1}^{∞} for which there exists i , $1 \leq i \leq n - k + 1$, such that $d(X_i^{i-1+k}, X_{n+1}^{n+k}) \leq D$ where D is the maximum distortion level.*

A variable-length compression code can be designed based on L_n . The code, roughly speaking, consists of pairs (pointer to a position i , length of L_n), if a sufficiently long L_n is found. Otherwise we leave the next L_n symbols uncompressed. We clearly need $\log n + \log L_n$ bits for the above code. The compression ratio r can be approximated by

$$r = \frac{\text{overhead information}}{\text{length of repeated subword}} = \frac{\log n + \log L_n}{L_n}, \quad (1)$$

and to estimate it one needs the probabilistic behavior of L_n . In [8, 9] it is proved that $L_n \sim \frac{1}{r_0(D)} \log n$ in probability (i.e., with high probability) where $r_0(D)$ is the so called generalized Rényi entropy (which could be views as follows: the probability of a typical ball in \mathcal{A}^n of radius D is approximately $2^{-nr_0(D)}$). From (1) we conclude that the compression ratio r is asymptotically equal to $r_0(D)$.

The above main idea is enhanced by several observations that constitute PMIC scheme. They are:

Additive Shift. It is reasonable to expect that in an image there are several substrings, say x_1^m, y_1^m , that differ only by *almost* constant pattern, that is, $y_i = x_i + c$ for $1 \leq i \leq m$ where c is not necessary a constant, but whose variation is rather small. In such a case we store the average difference c as well as a (*pointer, length*) pair, which enables us to recover

y_i from x_i (instead of storing y_i explicitly). In general, we determine the additive shift c by checking whether the following condition is fulfilled or not

$$\frac{1}{m} \left(\sum_{i=1}^m (x_i - y_i)^2 - \frac{1}{m} \left(\sum_{i=1}^m (x_i - y_i) \right)^2 \right) \leq D'$$

where D' is a constant. If the above holds, we compute the shift c as $c = \frac{1}{m} \sum_{i=1}^m (x_i - y_i)$. It can be easily verified that for $x_i = y_i + c$, and c a constant, the above procedure returns c . In passing, we should observe that this enhancement improves even *lossless* ($D = 0$) image compression based on the Lempel-Ziv scheme.

Reverse Prefix. We check for similarities between a substring in the uncompressed file and a *reversed* (i.e., read backward) substring in the database.

Variable Maximum Distortion. It is well known that human vision can easily distinguish an “undesired” pattern in a low frequency (constant) background while the same pattern might be almost invisible to humans in high frequency (quickly varying) background. Therefore, we used a low value of maximum distortion, say D_1 , for slowly varying background, and a high value, say D_2 , for quickly varying background. We automatically recognize these two different situations by using the derivative \mathcal{D}_{ij} of the image that is defined as

$$\mathcal{D}_{ij} = \frac{(x_{i+1,j} - x_{ij}) + (x_{i,j+1} - x_{ij})}{2}$$

where x_{ij} is the value of (i, j) pixel. In our implementation, we used the lower value of D_1 whenever $\mathcal{D}_{ij} \leq 3$ and the higher value of D_2 otherwise.

Max-Difference Constraint. Our code will also satisfy the additional constraint that $|x_i - \hat{x}_i| \leq DD$ where DD is a suitably chosen value. This additional constraint, which we call *max-difference* constraint, ensures that visually noticeable “spikes” are not averaged out of existence by the smoothing effect of the square error distortion constraint. We incorporate this max-difference constraint in the function $d(\cdot, \cdot)$ by adopting the convention that $d(x_i, \hat{x}_i) = +\infty$ if $|x_i - \hat{x}_i| > DD$, otherwise $d(x_i, \hat{x}_i)$ is the standard distortion as defined above (i.e., Hamming or square of difference).

Small Prefix. It does not make too much sense to store a *(pointer, position)* when the longest prefix is small. In this case, we store the original pixels of the image.

Run-Length Coding. For those parts of the picture that do not vary at all, or vary little, we used run-length coding: if the next pixels vary little, we store a pixel value and the number of repetitions.



(a)



(b)



(c)



(d)

Figure 1: Comparisons of different flavors of PMIC on the "Lena" image: (a) Classical PMIC (compression ratio equal to 4.3); (b) JPEG (compression ratio equal to 7.9); (c) PMIC with simple predictive coding (compression ratio equal to 7.9); (d) PMIC with column compression (compression equal to 5.3).

As mentioned above, in this paper we investigate an impact of prediction algorithms on PMIC. A simple prediction enhancement can work as follows (prediction loop – our main contribution of this paper – is described in depth in next sections):

Prediction. If we “reduce” the original image by taking only every second rows, then the size of the “reduced” image will be half of what the original one is. This way the compression can be performed on this “reduced” image allowing slight increase in the compression speed, while keeping roughly the same quality level as before. After decompression, the “reduced” image is “expanded” using classical 2-D linear prediction, that is, each row generates another one, which is predicted according to the scheme described below. Figure 1 shows two versions of the compressed Lena picture: one with PMIC, and the other with PMIC and predictive “reduction/expansion”. In passing, we point out that for high quality image compression, one can design a two-rounds approach where in the second round one sends the missing rows.

Finally, we also explore in this paper one more feature, namely:

Column compression. PMIC is performed on rows. In order to have it performed on columns, one simple way to proceed is to “transpose” the original image before compression. Indeed, the rows of the compressed “transposed” image are the columns of the original one. This algorithm has been performed on several different images, and this feature can sometimes increase either the compression ratio or the quality level, as shown in Figure 1.

Let us discuss algorithmic challenges of PMIC. It boils down to an efficient algorithm for the longest prefix of length L_n in yet uncompressed file. We present below one possible implementation (for others the reader is referred to [2]). Let x_1^n denote the database, $y_1^m = x_{n+1}^{n+m}$ denote the yet uncompressed file. As before, we write $d(x_i, y_j)$ for a distortion measure between two symbols, where $d(\cdot, \cdot)$ is understood to incorporate the max-difference criterion discussed earlier.

Algorithm PREFIX

Input: x_1^n and y_1^m

Output: Largest integer k such that, for some index t ($1 \leq t \leq n - m$), $d(x_t^{t+k-1}, y_1^k) \leq D$. The algorithm outputs both k and t .

Method: We compute, for all i, j S_{ij} = total distortion measure between x_i^{i+j-1} and y_1^j .

begin

Initialize all $S_{ij} := 0$.

for $i = 1$ **to** $n - m$ **do**

```

    for  $j = 1$  to  $m$  do
        Compute  $S_{ij} := S_{i,j-1} + d(x_{i+j-1}, y_j)$ 
    doend
doend
Let  $k$  be the largest  $j$  such that  $S_{ij} \leq jD$ , and let  $t$  be the corresponding  $i$ 
Output  $k$  and  $t$ 
end

```

The above can easily be modified to incorporate the enhancements discussed above (additive shift, etc.) and to use $O(1)$ variables rather than the S_{ij} array. In order to compress an $N \times N$ image we apply PREFIX several times to compress a row, which we call COMPRESS_ROW algorithm, and this is further use to compress a whole image in either COMPRESS_LONG_DATABASE (where the database sequence is of multiplicity of N , i.e., fN where f is a small integer) or COMPRESS_SHORT_DATABASE (where the database sequence is of length $O(1)$ but located just above the “point” of compression). In the former case the algorithmic complexity of compression is $O(N^4)$ while in the latter case it is $O(N^2 \log N)$ which is only $\log N$ away from the optimal complexity $O(N^2)$. In this paper we only use COMPRESS_SHORT_DATABASE algorithm.

3 Review of DPCM

In the following, $x_{i,j} = x_m$ stands for the gray-level value of the pixel currently in position $(i, j) = m$ in the $N \times N$ pixels original image, and $\hat{x}_{i,j} = \hat{x}_m$ is the gray-level value of the “predicted” (reconstructed) pixel of the reconstructed image. As seen in [11] and accordingly to Figure 2, the configuration of the 2-D predictor is as following:

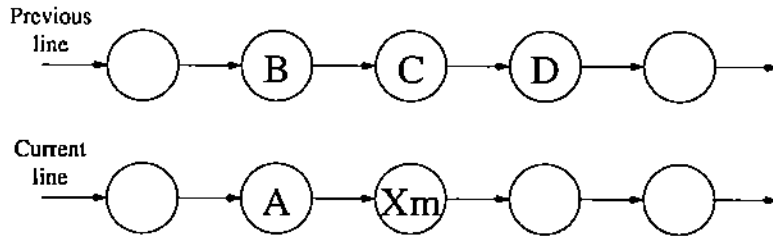


Figure 2: DPCM predictor configuration.

$$\hat{x}_m = 0.75A - 0.50B + 0.75C. \quad (2)$$

where $x_m = x_{i,j}$, $A = \hat{x}_{i,j-1}$, $B = \hat{x}_{i-1,j-1}$, and $C = \hat{x}_{i-1,j}$. In the above, e_m stands for the error value between the original and the reconstructed pixels:

$$e_m = x_m - \hat{x}_m. \quad (3)$$

Finally, e_m^* is the quantized value of e_m , as described in [11] from which Table 1 is drawn. In fact, we add an offset of 128 to e_m^* , making all of the error values positive (for an 8-bit original) so that they can be printed on a output device. Then:

Algorithm PREDICTION

Input: $x_{i,j} = x_m$, $\hat{x}_{i,j-1} = A$, $\hat{x}_{i-1,j-1} = B$, and $\hat{x}_{i-1,j} = C$ (see Fig. 2).

Output: e_m^* . **Method:** We compute a first \hat{x}_m , then e_m and e_m^* . Eventually, we update the value of \hat{x}_m .

begin

 Compute \hat{x}_m accordingly to Eq. 2.

 Clip \hat{x}_m to the range $[0,255]$.

 Compute $e_m := x_m - \hat{x}_m$.

 Compute $e_m^* := \text{Quantize}(e_m)$.

 Upgrade \hat{x}_m by computing $\hat{x}_m := \hat{x}_m + e_m^*$.

 Clip \hat{x}_m to the range $[0,255]$.

end

i	$(d_i, d_{i+1}) \rightarrow r_i$	Probability	Huffman Code
0	$(-255, -16) \rightarrow -20$	0.025	111111
1	$(-16, -8) \rightarrow -11$	0.047	11110
2	$(-8, -4) \rightarrow -6$	0.145	110
3	$(-4, 0) \rightarrow -2$	0.278	00
4	$(0, 4) \rightarrow 2$	0.283	10
5	$(4, 8) \rightarrow 6$	0.151	01
6	$(8, 16) \rightarrow 11$	0.049	1110
7	$(16, 255) \rightarrow 20$	0.022	111110

Table 1: 8-level Lloyd-Max quantizer for the “Lena” image.

The DPCM algorithm is summarized in Figure 3. We observe that it applies to every pixel of the image. That leads to the following algorithm:

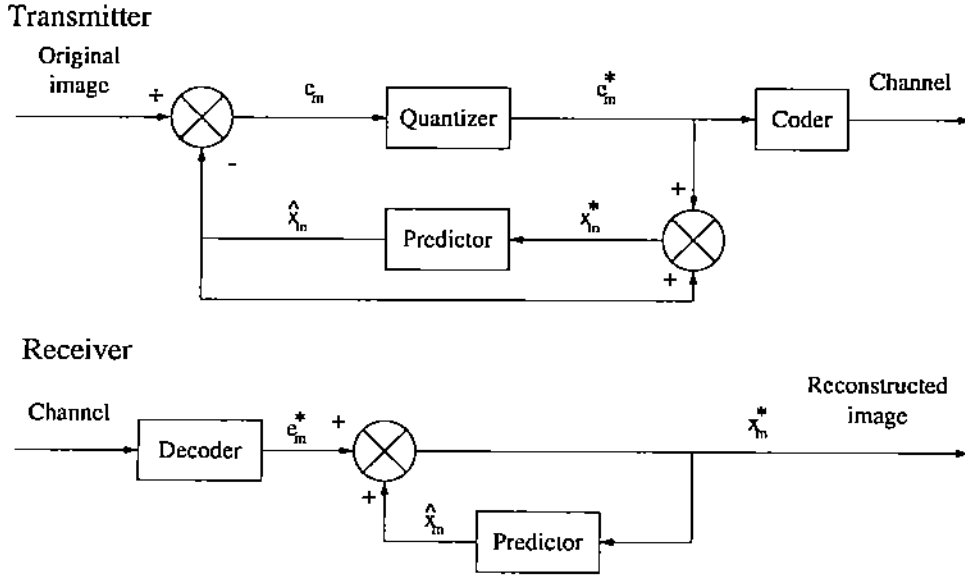


Figure 3: DPCM block diagram.

Algorithm PREDICTION LOOP

Input: $x_{i,j} = x_m$, for all $(0 \leq i \leq N - 1)$ and $(0 \leq j \leq N - 1)$.

Output: e_m^* , for all $(0 \leq i \leq N - 1)$ and $(0 \leq j \leq N - 1)$.

Method: We use PREDICTION to compute e_m^* for each pixel.

begin

Initialize $\hat{x}_m = x_m$ and $e_m^* = x_m$ for all $(0 \leq i \leq N - 1)$ and $j = 0$.

for $j = 1$ **to** $N - 1$ **do**

for $i = 0$ **to** $N - 1$ **do**

Call PREDICTION on $x_{i,j} = x_m$, $\hat{x}_{i,j-1} = A$, $\hat{x}_{i-1,j-1} = B$, and
 $\hat{x}_{i-1,j} = C$ (see Fig. 2).

doend

doend

end

From Figure 3 one concludes that the prediction (reconstructed pixel) \hat{x}_m for the transmitter is exactly the same as the one used by the receiver. They both need, and only need, the quantized difference e_m^* . The transmitter puts this difference in a file, whereas the receiver reads this difference from the file.

Finally, e_m^* , which is the quantized difference for each pixel, and the whole picture (formed with these quantized differences) is compressed with Huffman code.

4 New Algorithm: PMIC with DPCM

Like in Huffman compression (which is part of DPCM), the PMIC compression algorithm should be performed on the quantized differential image. However, the above algorithms are well adapted to Huffman coding, because they are on a pixel-by-pixel basis. Unfortunately, the PMIC algorithm, proceeds several pixels at a time (i.e., the longest prefix found in the database). Besides, we do not know in advance what the length of this prefix will be. But, there is a way around all of those problems. In fact, if we consider the PREDICTION algorithm to be performed, not on a pixel basis, but on a cell (which is, in the case of DPCM, one single pixel) basis, then this algorithm needs just a few adaptations in order to be suited for PMIC. Indeed, the cell in PMIC becomes naturally the longest prefix found in the database.

These considerations lead to the following two algorithms:

Algorithm DIFFERENTIAL_PREFIX

Input: \hat{x}_1^n , ex_1^n (where $n = fN$), and y_1^N

Output: Largest integer k such that, for some index t ($1 \leq t \leq n - N$), $d(ex_t^{t+k-1}, ey_1^k) \leq D$. The algorithm outputs both k and t , as well as \hat{y}_1^N and ey_1^N , both returned by the call to the PREDICTION_LOOP algorithm.

Method: We first use PREDICTION_LOOP to form a differential row, then we compute, for all i, j , S_{ij} = total distortion measure between ex_i^{i+j-1} and ey_1^j .

begin

 Call PREDICTION_LOOP on x_1^N

 Let \hat{y}_1^N and ey_1^N be returned by this call to PREDICTION_LOOP.

 Initialize all $S_{ij} := 0$.

for $i = 1$ **to** $n - N$ **do**

for $j = 1$ **to** N **do**

 Compute $S_{ij} := S_{i,j-1} + d(ex_{i+j-1}, ey_j)$

doend

doend

 Let k be the largest j such that $S_{ij} \leq jD$, and let t be the corresponding i

Output k and t

end

One should note that the PREDICTION_LOOP algorithm is here used on generally more pixels than needed, since it is used on N pixels, and that the longest prefix will have a size $\leq N$.

Algorithm COMPRESS_DIFFERENTIAL_ROW**Input:** \hat{x}_1^n , ex_1^n (where $n = fN$), y_1^N .**Output:** A compressed version of ey_1^N , in the form of (*pointer, length*) pairs, and the new reconstructed portion, \hat{y}_1^N , of the database.**Method:** We use PREFIX to “peel off” a prefix of the row being compressed, and repeat on the remaining portion of that row until we use it all up.**begin** Initialize $i := 0$. Repeat the following until $i \geq N$: Call PREFIX on \hat{x}_1^n , ex_1^n and y_{i+1}^N . Let k and t , \hat{y}_{i+1}^N and ey_{i+1}^N , be returned by this call to PREFIX: If k is small (say, ≤ 4) then ey_{i+1}^{i+k} is stored explicitly, else ey_{i+1}^{i+k} is stored as a (*pointer, length*) pair, Compute $\hat{y}_{i+1}^{i+k} := \hat{y}_{i+1}^{i+k} + ey_{i+1}^{i+k}$ (addition of vectors). Set $i := i + k$ **end**

We have used here the notation ex and ey for x and y , as they are understood in the COMPRESS_ROW algorithm of [2] and discussed briefly above, except that what is now compressed is the quantized differential image, whence the e before x and y . Therefore, \hat{x}_1^n represents the reconstructed (“predicted”) database (and is, in fact, the image as it will be again after decompression); ex_1^n means the database of the differential image (image actually being compressed); y_1^N is the currently processed row of the original image; ey_1^N is the “differential” row currently being compressed, that is, the differential pendant of y_1^N ; and \hat{y}_1^N is the new portion of the reconstructed (“predicted”) database. Thus, \hat{y} leads to \hat{x} , and ey gives ex .

Finally, we present some experimental results. We summarize them in Tables 2—4 where JPEG, PMIC with constant and variable D , and PMIC-PL (PMIC with Prediction Loop) are compared for three images, namely: “Lena” image, “Basselope” image (a graphic image) and “San Francisco” image (a photographic image). We conclude that prediction, as discussed in Section 2, can lead to substantial speed up of compression time, better compression time without significant deterioration of image quality. More sophisticated PMIC-PL can lead to further improvements, as our preliminary results suggest. However, results in Tables 2—4 are, in fact, worse than expected. We believe they originate from

Table 2: “Lena” image compressed by JPEG (quality=57), PMIC with constant D ($D = 155$, $DD = 20$), PMIC with variable D ($D1 = 500$, $D2 = 55$, $DD = 22$), and PMIC-PL ($D1 = 600$, $D2 = 50$, $DD = 16$).

	JPEG	Const D	Var D	PMIC-PL
Compression ratio	10.03	9.99	10.01	10.04
Bit rate (bits/pixel)	0.8	0.8	0.8	0.8
RMSE (0-255)	4.65	8.90	8.44	15.97
PSNR (dB)	34.78	29.14	29.61	24.06

Table 3: “Basseloop” image compressed by JPEG (quality=57), PMIC with constant D ($D = 800$, $DD = 38$), PMIC with variable D ($D1 = 800$, $D2 = 100$, $DD = 39$), and PMIC-PL ($D1 = 1000$, $D2 = 45$, $DD = 15$).

	JPEG	Const D	Var D	PMIC-PL
Compression ratio	9.96	10.04	10.04	9.96
Bit rate (bits/pixel)	0.8	0.8	0.8	0.8
RMSE (0-255)	9.07	12.22	8.44	78.89
PSNR (dB)	28.97	26.39	29.61	10.19

Table 4: “Lena” image compressed by JPEG (quality=21), PMIC with constant D ($D = 400$, $DD = 38$), PMIC with variable D ($D1 = 500$, $D2 = 55$, $DD = 22$), and PMIC-PL ($D1 = 600$, $D2 = 50$, $DD = 16$).

	JPEG	Const D	Var D	PMIC-PL
Compression ratio	10.03	10.00	9.95	10.02
Bit rate (bits/pixel)	0.8	0.8	0.8	0.8
RMSE (0-255)	7.96	13.92	12.87	20.41
PSNR (dB)	30.11	25.26	25.94	21.94

the fact that we use variable-D scheme which seems to be unsuited for the predictive loop (the derivative is actually done on the original image, and not on the differential image, as it should be). This might be an interesting point for future research (i.e., to implement a good derivative scheme on the differential image). Then, we believe we can achieve much more substantial improvements. This will be reported in our journal version of this paper.

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